

High-throughput label-free particle separation in viscoelastic fluids via elasto-inertial focusing

Student: Xinyu Lu (PhD)

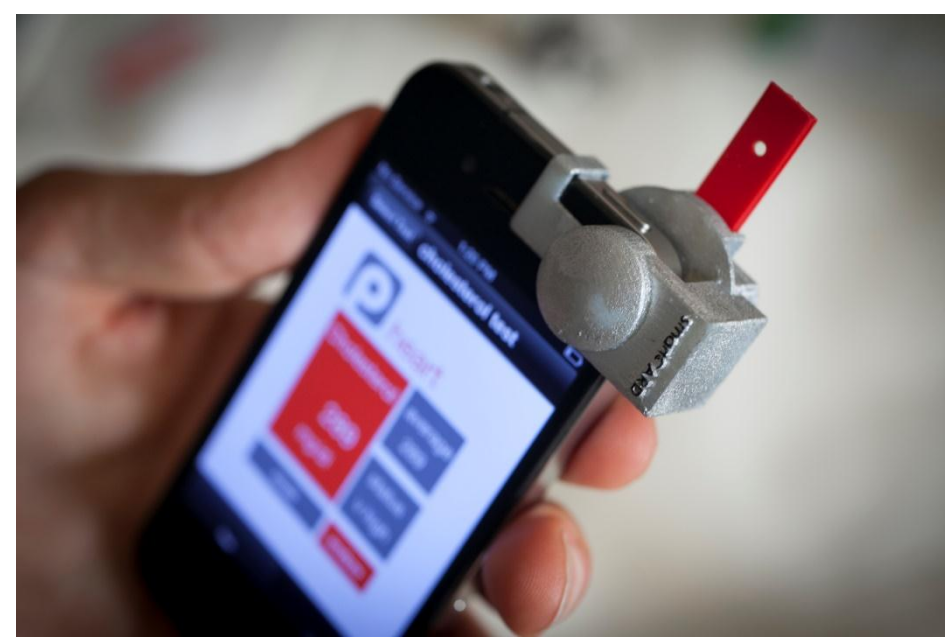
Advisor: Xiangchun Xuan, Associate Professor
Mechanical Engineering, Clemson University, SC



1. Motivation

Lab-on-a-Chip (LOC)

- Developed for chemical and biomedical application
- Reduces a laboratory to the size of a credit card
- Compatibility with biological analysis

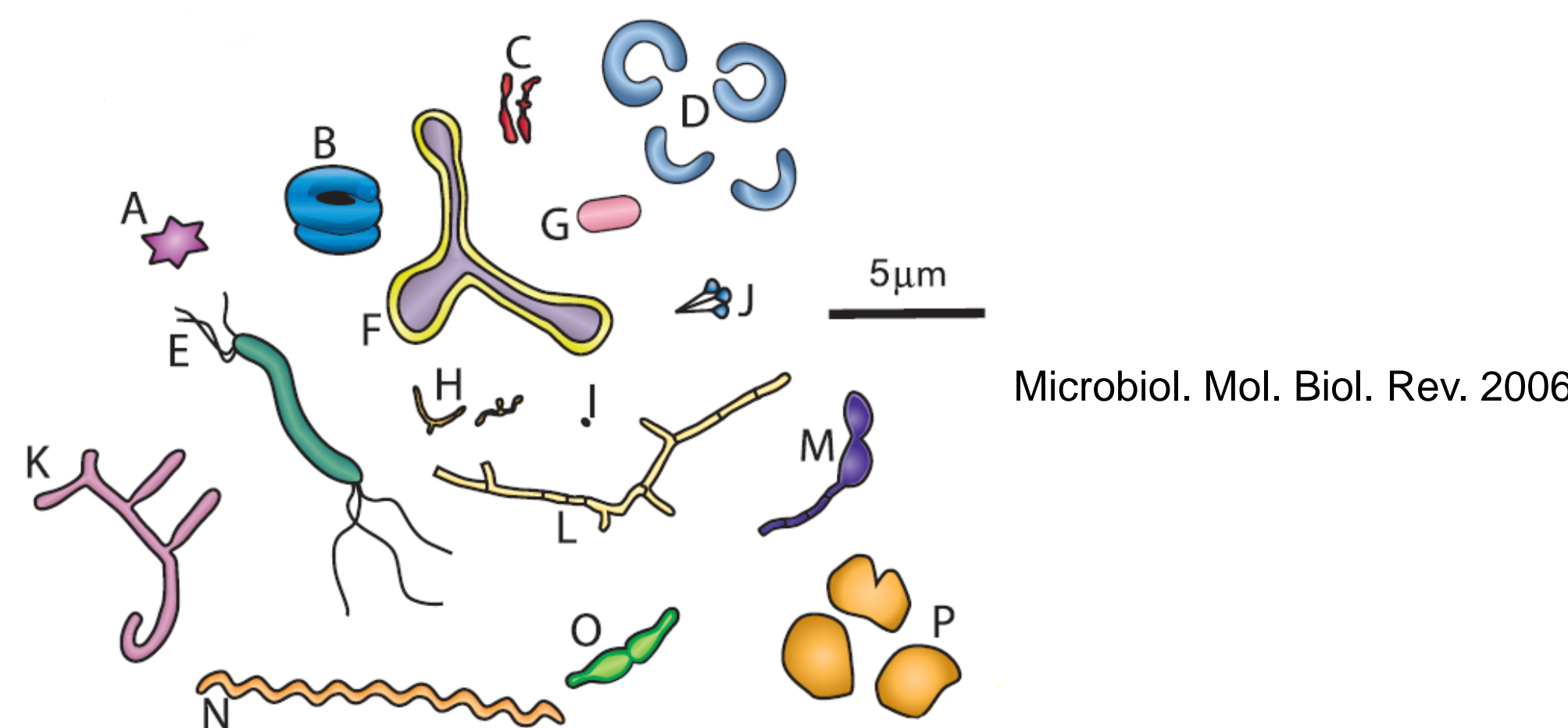


Smartphone camera clip-on and app for at-home cholesterol testing, MedCityNews, 2013



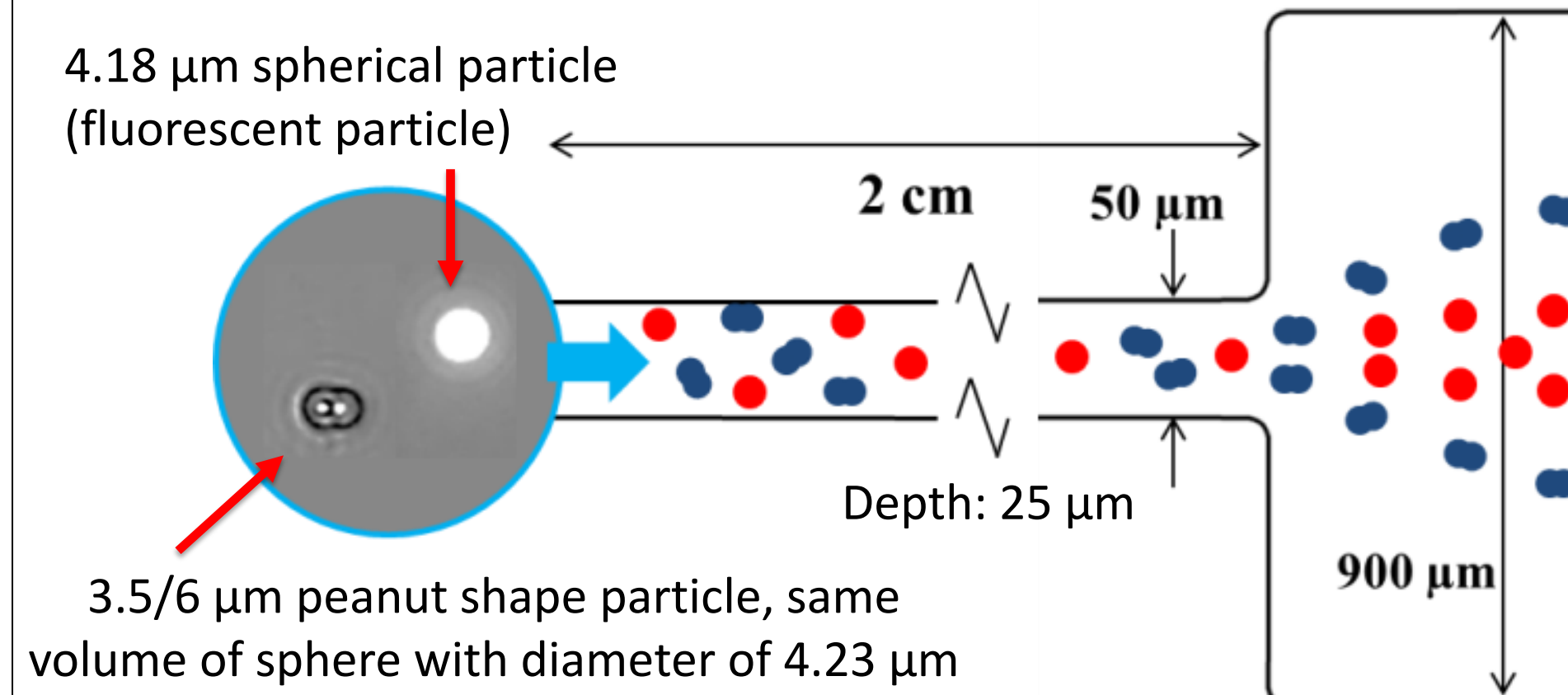
Small biomedical chip, ©BMNL Group

- Bodily fluids (e.g., blood and saliva) and polymer solution exhibit non-Newtonian behaviors such as viscoelasticity that few people studied
- Cells and bacteria have different sizes and a variety of shapes, which can be used as markers of sorting



2. Experimental design

- Size/shape-based separation in non-Newtonian fluid through 50 μm-wide straight microchannels



Schematic diagram of shape-based separation

- Size-based separation is in a similar 50 μm-wide channel for spherical particles with diameters of 3 and 10 μm

3. Intellectual Merit and Broader Impacts

- We explore the elasto-inertial flow with Reynolds number near order 1 and Weissenberg number ($Wi = \text{shear rate} \cdot \text{relaxation time} = \dot{\gamma} \cdot \lambda$) near order 10
- This approach is continuous, passive, simple in channel design and in control, and high purity (>95%)
- It can be used in applications of particle/cell separation and diagnosis for spheres with different sizes or those with similar volume but different shapes

4. Theory

Non-Newtonian fluid

- Different from Newtonian fluid
 - Viscoelastic effect
 - Shear-thinning/thickening effect (weak in this project)
- In our experiment, non-Newtonian fluids were prepared by dissolving 1000ppm Poly(ethylene oxide) (PEO) powder (average molecular weight is $2e6$)
- Oldroyd-B model is widely used to model dilute PEO fluid

3D Stationary model was built in CONSOL

$$\rho(\mathbf{u} \cdot \nabla) \mathbf{u} = \nabla \cdot (-p\mathbf{I} + \mu[\nabla \mathbf{u} + (\nabla \mathbf{u})^T] + \mathbf{T})$$

$$\mathbf{T} + \lambda \overset{\nabla}{\mathbf{T}} = \eta[\nabla \mathbf{u} + (\nabla \mathbf{u})^T]$$

where

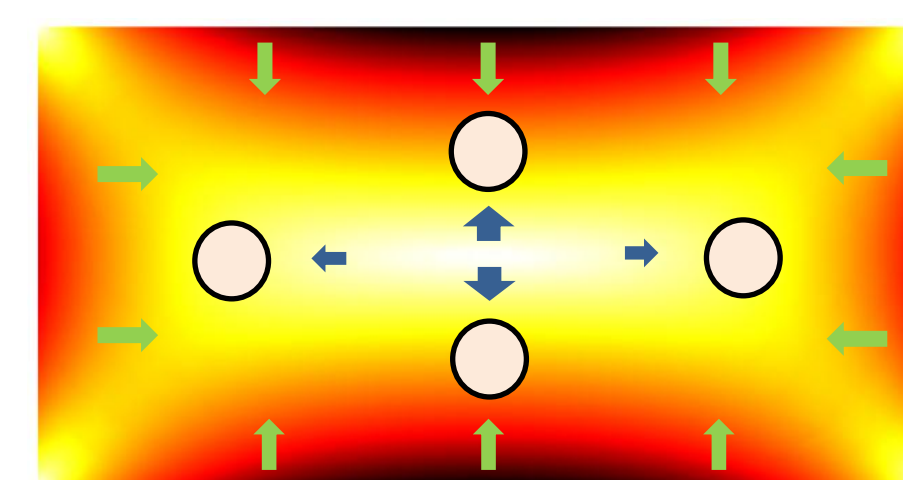
$$\overset{\nabla}{\mathbf{T}} = \frac{\partial \mathbf{T}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{T} - [(\nabla \mathbf{u}) \mathbf{T} + \mathbf{T} (\nabla \mathbf{u})^T]$$

μ : solvent viscosity η : polymer viscosity $\mu_0 = \mu + \eta$

Extra Stress

Particle equilibrium positions for sphere

Inertia



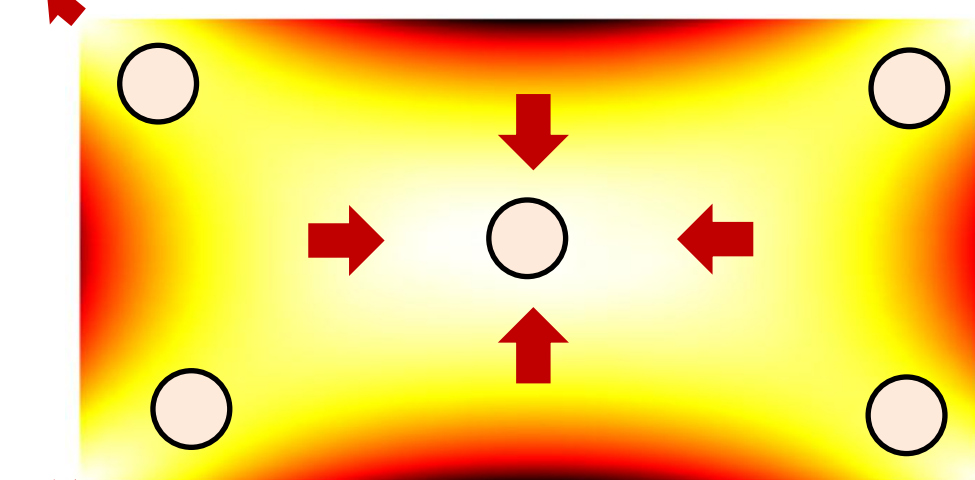
Shear rate distribution on the cross section (Newtonian $Re \sim o(1)$)

Note: the background shows the simulated shear rate/first normal stress difference intensity (the redder the higher).

Wall lift force: pushes the particles away from the walls

Shear rate force: pushes the particles away from the low shear rate regions

Viscoelasticity



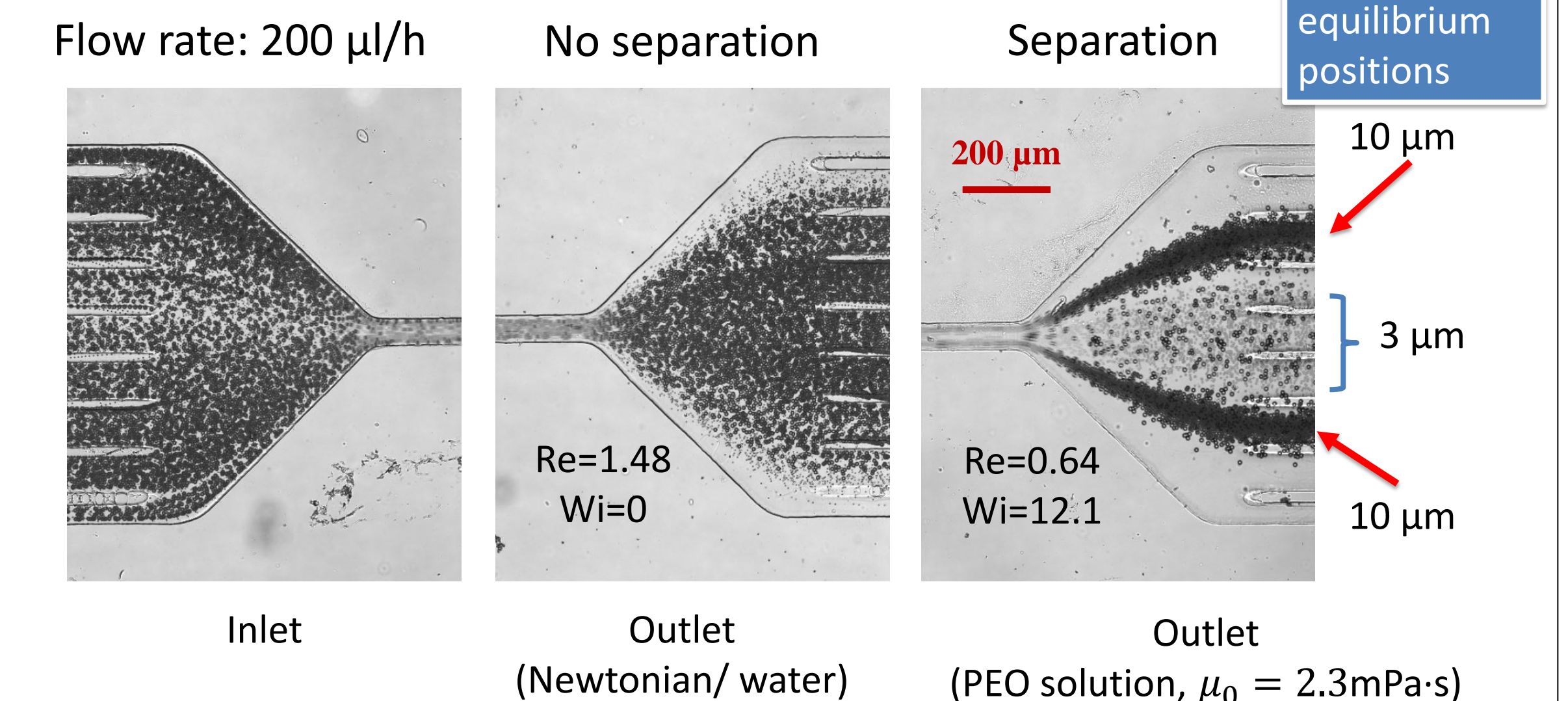
First normal stress difference N_1 ($\sigma_{xx} - \sigma_{yy}$) distribution (Oldroyd-B model, $Wi \sim o(10)$)

Viscoelastic lift force: pushes the particles towards the low first normal stress difference regions.

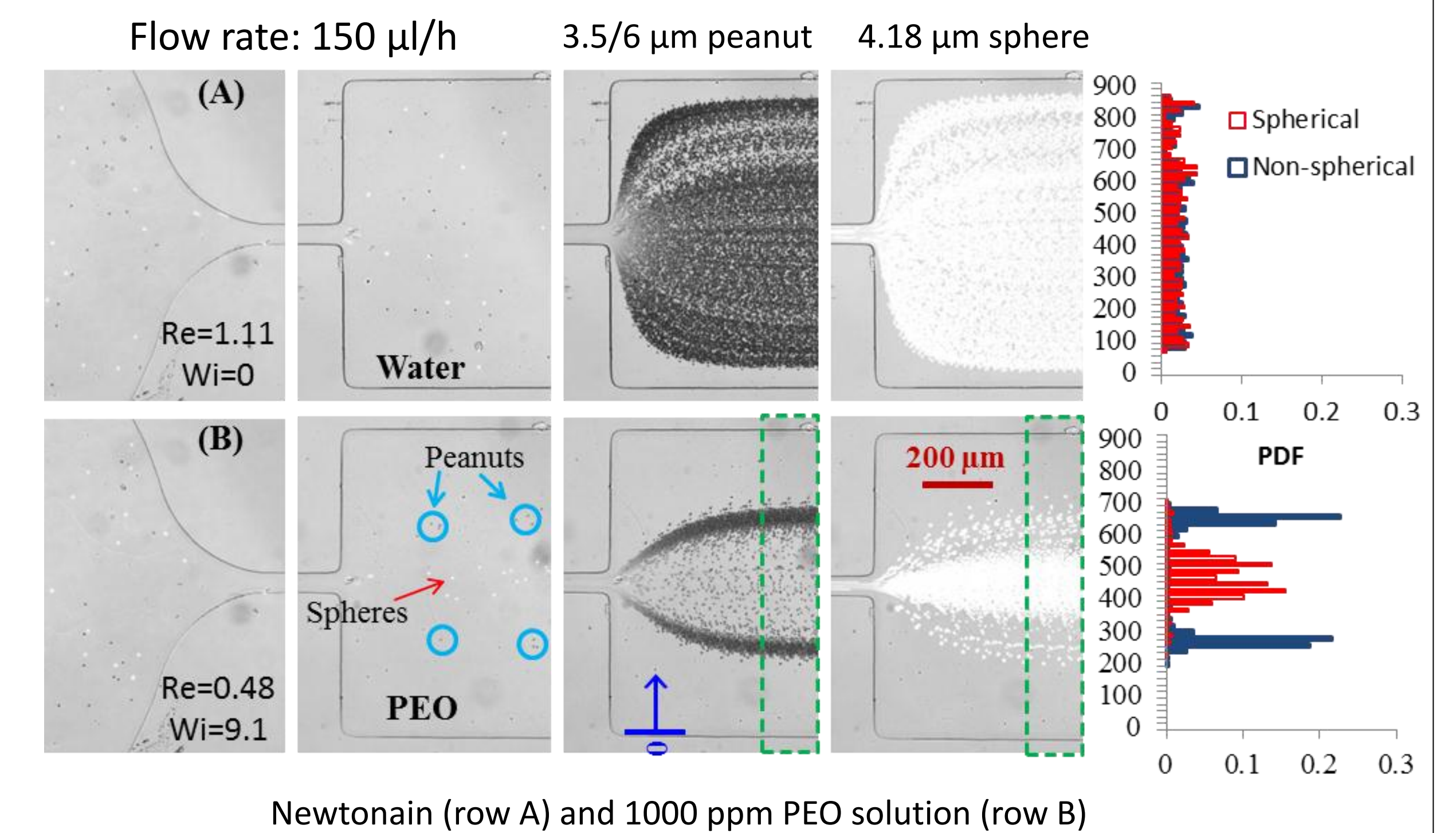
$$F_{VE} \sim a^3 \nabla N_1$$

5. Results

Size-based (3 and 10 μm) particle separation



Shape-based (sphere and peanut) particle separation



- Peanut rotates much slower in non-Newtonian fluid than in Newtonian solution
- shape-dependent elasto-inertial lift-induced particle migration is speculated to correlate with the rotation effects and as well the effective diameter of non-spherical particles

6. Conclusion and future plan

- In a range of $Re \sim o(1)$, the pure inertial lift barely varies on particle motion between different sizes/shapes, but the elasto-inertial effect does
- Size and shape-based separations are achieved in viscoelastic fluid
- To further study the shape-dependent elasto-inertial lift, we are currently fabricating ellipsoidal particles of various aspect ratios for additional test; the simulation of particle-fluid interaction is in process